

# Complex Metaheuristics <sup>☆</sup>

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## Abstract

Complexity is a prevalent feature of numerous natural and artificial systems and as such has attracted much scientific interest in the last decades. The pursuit of computational tools capable of analyzing, modeling or designing systems exhibiting this complex nature –in which the properties of the system are not evident at the bottom level but emerge from its global structure– is a major issue. Metaheuristics can play here an important role due to its intrinsic adaptability and powerful optimization capabilities. In many regards, metaheuristics are also examples of complex systems since their behavior emanates from the orchestrated interplay of simpler algorithmic components. This bidirectional connection between metaheuristics and complex systems offers numerous avenues for fruitful research.

*Keywords:* complex systems, complex networks, metaheuristics, multiagent systems, multi-scale, multi-physics and multi-goal systems.

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## 1. Introduction

Complex systems are ubiquitous in physics, economics, sociology, biology, computer science, and many other scientific areas [1, 2, 3]. Typically, a complex system is composed of smaller aggregated components, whose

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interaction and interconnectedness are non-trivial (*e.g.*, interactions can be high-dimensional and non-linear, can include feedback loops, and the connectivity can exhibit non-trivial topological features such as power-law degree distribution [4], and high clustering coefficient [5]). This leads to emergent properties of the system, not anticipated by its isolated components. Furthermore, when the system behavior is studied from a temporal perspective, self-organization patterns are not unusual [6, 7].

Studying complex systems often requires composite strategies that employ various different algorithms to solve a single difficult problem. Components of such strategies may solve consecutive phases leading to the main goal (for example, consider an oil deposit exploration strategy composed of a complex memetic search algorithm [8] and of a direct FEM solver), may be used to approach particular sub-tasks from different perspectives (as, for example, in multi-scale approaches [9]), or may solve the main problem in different ways that are aggregated to form the final solution (as, for example, in hyper-heuristics [10], island GAs [11] or multi-physics approaches [12]).

This thematic special issue revolves around the intersection of metaheuristic optimization techniques and complex systems from two different perspectives, namely the use of metaheuristics as a tool for analyzing, modeling or designing complex systems, or the utilization of metaheuristics approaches which are themselves complex systems due to its particular internal structure. We have gathered six papers [13, 14, 15, 16, 17, 18] targeted to cover algorithmic and implementation aspects of such complex metaheuristics in both discrete and continuous domains, as well as applications to complex systems. Some contributions to this thematic special issue are extended versions of results communicated at the EvoCOMPLEX track of the EvoApplications conference [19], held in Copenhagen, 8-10 April 2015 as a part of the EvoStar event<sup>1</sup>.

## 2. An Overview of this Special Issue

The papers included in the special issue tackle a variety of topics. Three of them [14, 15, 16] deal with multi-objective optimization, underlining the polyhedral nature of many complex problems. Complex networks [20] are prominently featured in one contribution [13] and other different hard complex optimization problems are considered in four contributions [14, 15, 16, 17]. Finally, one of the contributions [18] tackles the use of agent-based

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<sup>1</sup><http://www.evostar.org>

metaheuristic computing, a prime example of complex collective system [21] – see also [22]. A more detailed introduction to these papers is provided next.

Li et al. [16] consider an optimization approach termed chemical reaction optimization which draws inspiration from molecules transitioning to lower energy states by collisions. In an analogy to chemical reactions, each molecule carries some energy which changes upon collisions but is globally conserved. The role of energy supporting certain types of reactions bear some resemblance with the homonym concept in multi-agent systems. This approach is extended to multi-objective optimization problems by considering the Tchebycheff aggregation of different single-objective functions. This approach is benchmarked against other multi-objective evolutionary algorithms on the ZDT and DTLZ functions.

Harrison et al. [13] focus on the analysis and modeling of complex networks. Considering the different structural properties that can be measured for a given network, they address the question of which ones can be used as good estimators of this structure in the sense of discriminating between networks generated using different network models. This issue is tackled using a meta-analysis of network properties based on Fischer’s method, whose outcome is subsequently used as the fitness function of a genetic-programming system aimed to generate networks structurally similar to a certain target network. This approach is validated using both artificial and real-world complex networks.

Hernández et al. [14] also consider a multi-objective problem, in this case in the context of computer vision and more precisely in object classification tasks. They build upon a model known as artificial virtual cortex, which approaches the object recognition problem based on the human visual cortex by combining a psychological model and a neurophysiological model. This model is extended in this work in order to be able to provide both an image descriptor vector for classification and the location of objects within the image. This is done by means of the brain programming paradigm, an approach related to genetic programming but featuring a complex heterogeneous multi-tree representation for individuals. The approach is benchmarked against other state-of-the-art techniques on two standard image databases.

Turek et al. [18] focus on the parallelization of agent-based metaheuristic computing. To this end, they consider a framework in Erlang, the concurrent functional programming language. This framework is deployed in a multi-core computing system, aiming to study the scalability of three different implementations when up to 64 cores are used. They study how different

algorithmic aspects such as representation or asynchronicity influence performance. After introducing different optimizations in the system, they validate the performance of the approach on a complex real-world problem related to crossroad light management in a simulated traffic system.

Łazarz et al. [15] delivers a study of solving multi-objective optimization problems by using a hierarchy of demes (the so-called Hierarchic Genetic Strategy – HGS). A new invented maturing mechanism is proposed in order to both improve efficiency and reducing the redundancy of computations. The proposed strategy is especially well fitted for ill-conditioned multi-objective problems and can significantly decrease the computational cost in the case for which the cost of single fitness evaluation depends on the solution accuracy. The proposed strategy was exhaustively tested with six various selections preferring individuals closer to the Pareto set. The test results for many benchmarks were compared to the results of single- and multi-deme state-of-the-art MOEA algorithms.

Obuchowicz and Smółka [17] study the idea of improving the exploratory skills of complex multi-deme metaheuristics by introducing mutation based on stable probability distributions with low stability index  $\alpha$ . This improvement is used for solving an advanced ill-conditioned inverse parametric problem connected to oil and gas resource exploration. An interesting aspect of this work is the method used for intelligently scaling the hard-computing simulation module that evaluates the fitness function. The experimentation indicates how this improved mutation operator can contribute to finding more solutions in less computational time and in a more predictable way.

### 3. Perspectives

The research results presented in the special issue show clear directions for future developments in the area of complex systems and nature-inspired algorithms. They decidedly will go towards new algorithmic inventions allowing for handling ill-conditioned problems, featuring multimodality and areas of insensitivity and uncertainty of the search objectives. Another important direction of development will lead to more effective software architectures, that allow solving larger challenging problems. One of the recurring ideas is to couple hard- and soft-computing components resulting in complex systems themselves, e.g. multi-deme genetic searches with the twin-grid, sophisticated *hp*-FEM adaptive solvers. Complex collective systems such as agent-based metaheuristics or chemical reaction optimization algorithms are also ripe for success in solving hard optimization tasks. From an applied

point of view, complex systems are plentiful in appealing optimization problems of real-world interest and enormous difficulty. Both the analysis of complex networks and tasks related to human-like vision systems can be successfully tackled with nature-inspired algorithms, as shown here. Needless to say, there are many other complex domains such as cellular automata [23] or social computational systems [24], just to mention a few, in which this kind of techniques can be deployed, thus bringing many interesting avenues for further research.

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