

Graphical Representation of Authorization Policies for Weighted Credentials

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Introduction

- Make use of weighted credentials to define authorization and delegation relationships.
- Define three main indexes which help on deciding authorization requests.
- Define authorization flexible policies
- Define graphical representation for:
 - Credentials
 - Authorization “power” between pairs of entities
 - Authorization policies

Credentials

- **Issuer**
- **Subject**
- **Type**
 - *Weight*: real number in $[0,1]$
 - *Delegable*: 1 for Delegation, 0 for Authorization
 - *Sign*: 1 for positive, 0 for negative
- **Right**
 - *Resource*
 - *Access Mode or Operation*

Kind of Credentials



Positive
Delegation



**Positive
Authorization**



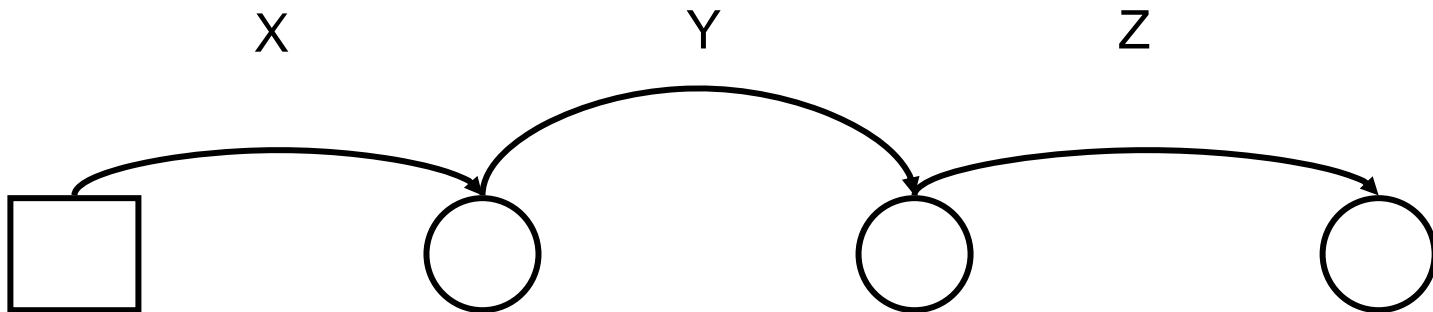
Negative
Delegation



Negative
Authorization

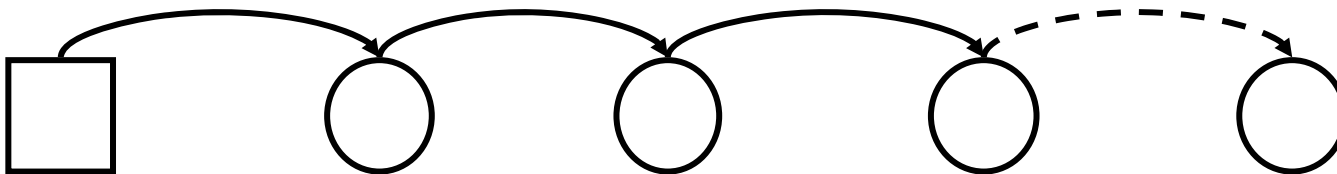
Paths or Chains of Credentials

- Source of Authorization (SOA)
- Credentials or edges
- Final entity
- Weights



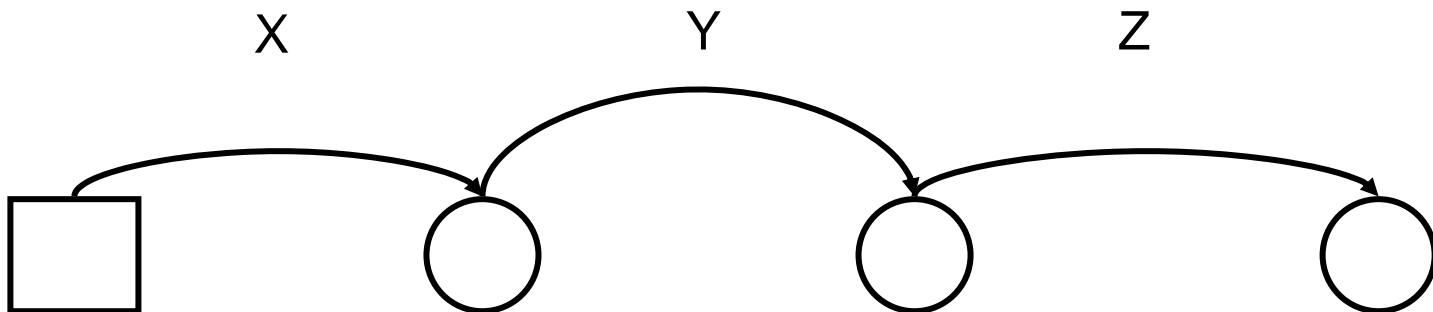
Paths or Chains of Credentials

- Delegation Path
 - All credentials in the path are delegation credentials
- Authorization Path
 - Delegation path + Authorization credential



Metrics over Paths

- Multiplicative: $X \cdot Y \cdot Z$
- Additive: $X + Y + Z$
- Minimum: $\text{Min}(X, Y, Z)$
- Maximum: $\text{Max}(X, Y, Z)$



Measuring Authorization

 L_{AB}

Is defined as the lowest weight over the weight of all authorization paths from A to B.

 H_{AB}

Is defined as the greatest weight over the weight of all authorization paths from A to B.

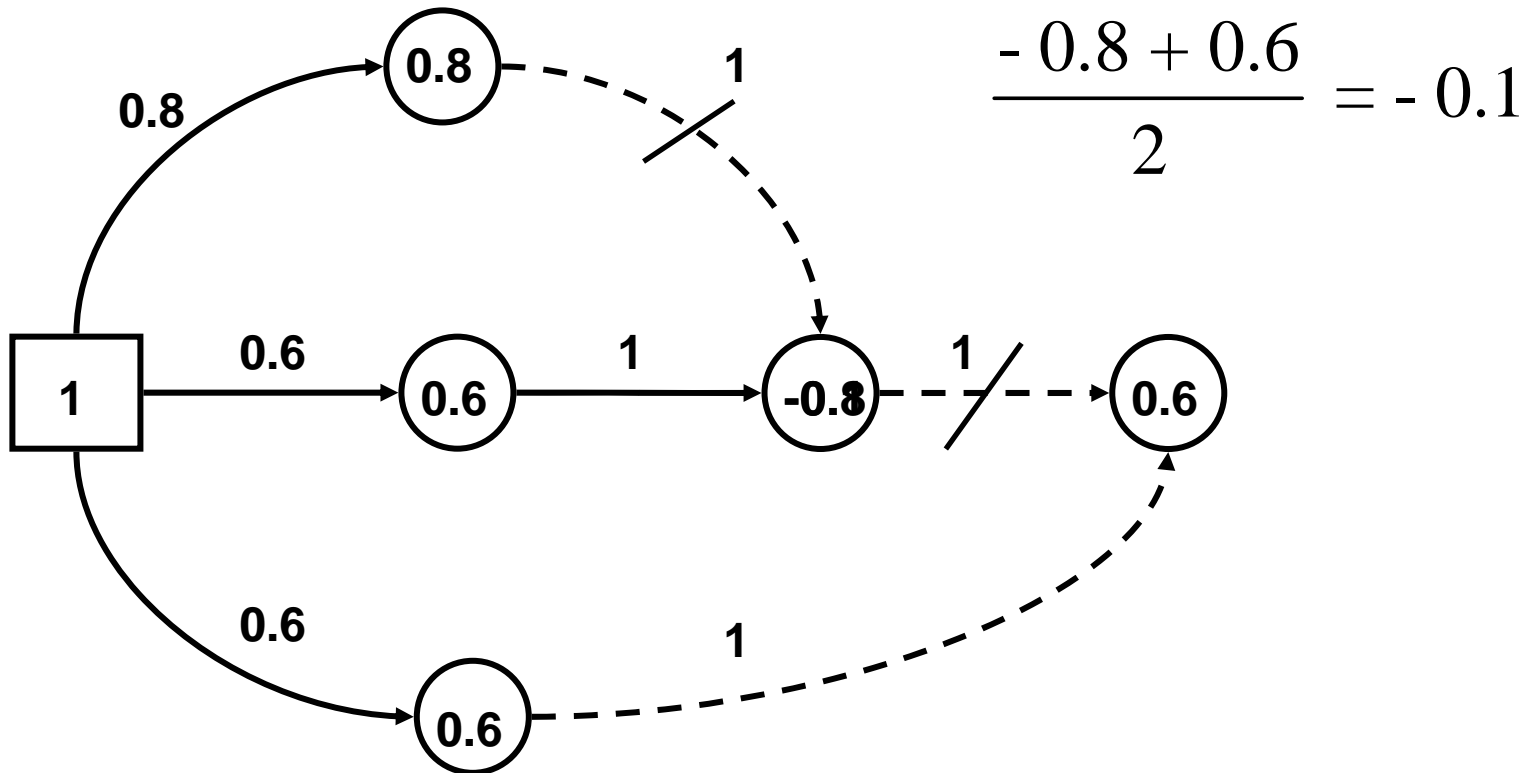
Mean Index (M_{AB})

- Initialization
 - $m(a,x)=0$ for all $x \neq a$, $m(a,a)=1$ and $p=a$
- Loop over all neighbors, p' , of p
 - If the credential from p' to p is a delegation credential:

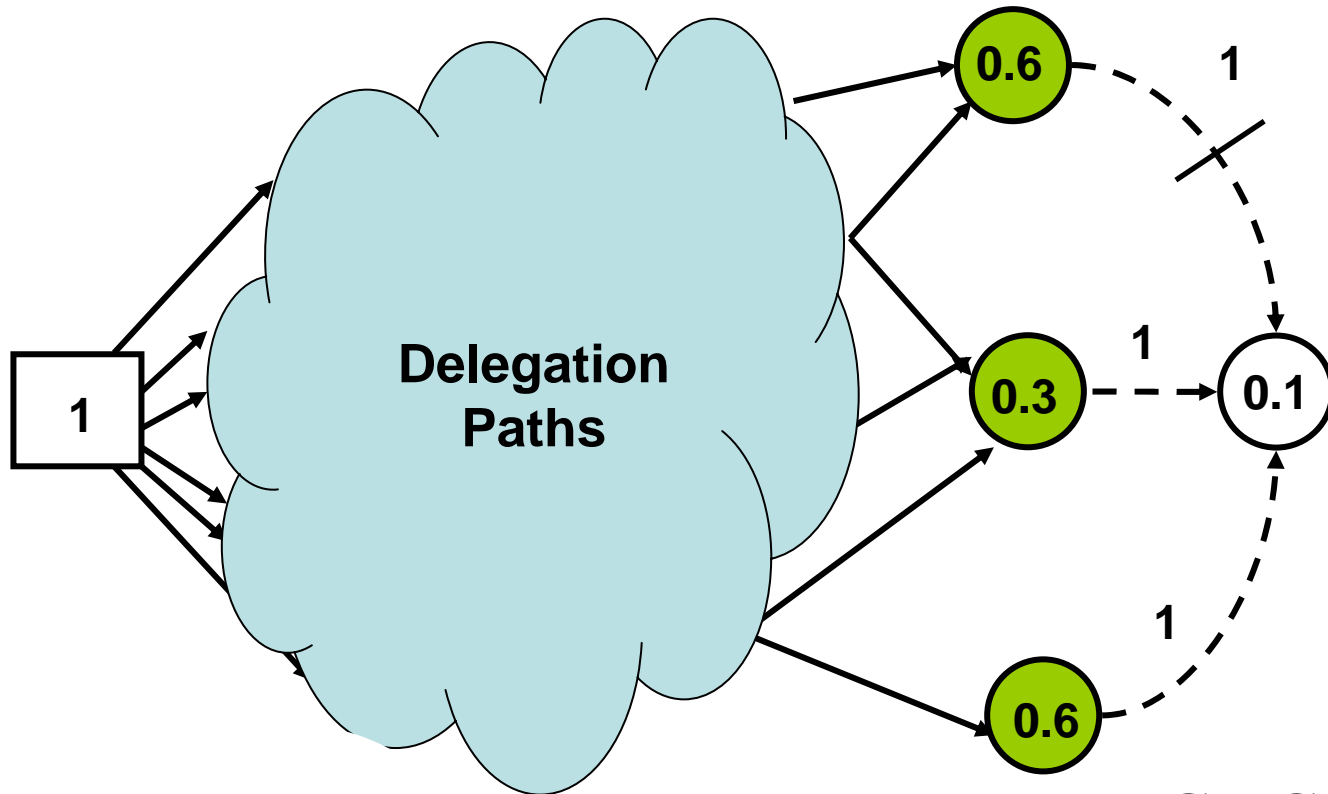
$$m(a,p')=m(a,p)*|pp'|*sign(pp')+m(a,p')$$
 - If the credential from p' to p is a negative authorization credential:

$$m(a,p')=m(a,p') - m(a,p)*|pp'|$$
- Expand a neighbor p' with $m(a,p')>0$, in decreasing order of $m(a,p')$.

Mean Index



x-Percentage Interval



There are 3 authorization paths, C_1, C_2, C_3 ,
with $|C_1| = -0.6, |C_2| = 0.3, |C_3| = 0.6$

so we get: $L_{AB} = -0.6$ $M_{AB} = 0.1$ $H_{AB} = 0.6$

x-Percentage Interval

Then the **x-percentage interval** is defined as

$$[L_{AB}^x, H_{AB}^x] = [\max(L_{AB}, M_{AB} - r_x), \min(H_{AB}, M_{AB} + r_x)]$$

where $r_x = \min \{ y \in \mathbb{R} : [M_{AB} - y, M_{AB} + y] \text{ includes the } x\% \text{ of weights} \}$

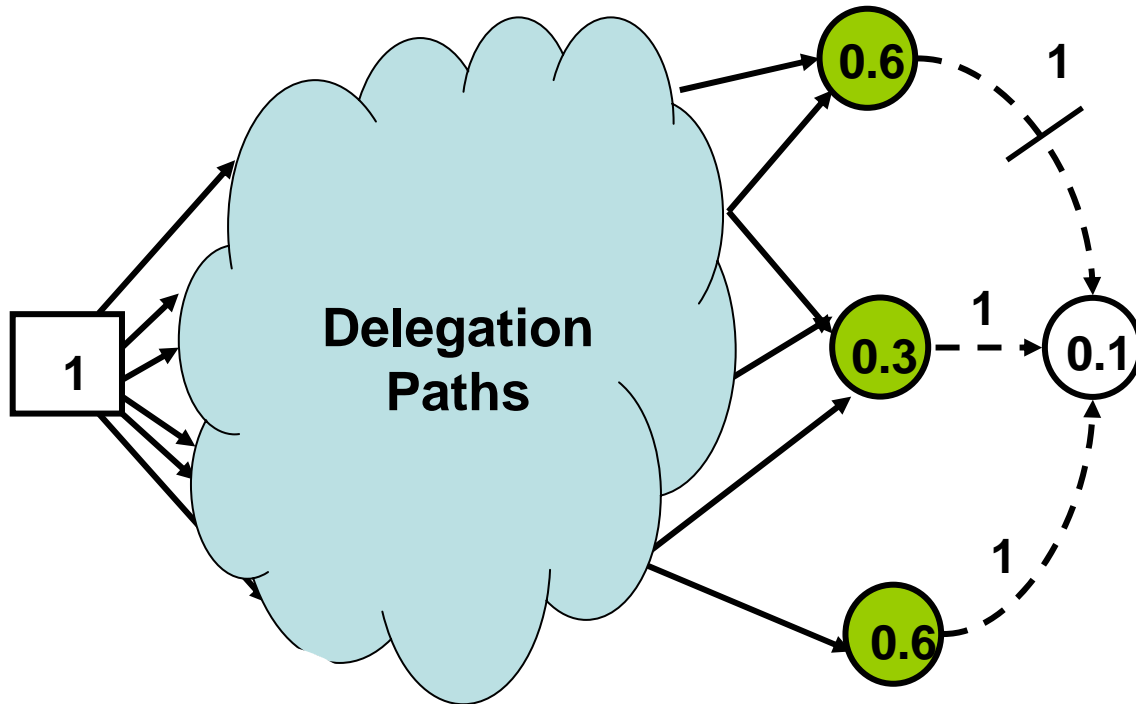
All defined indexes are related in this way

$$-1 \leq L_{AB} \leq L_{AB}^x \leq M_{AB} \leq H_{AB}^x \leq H_{AB} \leq 1$$

$$\lim_{x \rightarrow 100\%} L_{AB}^x \downarrow L_{AB}$$

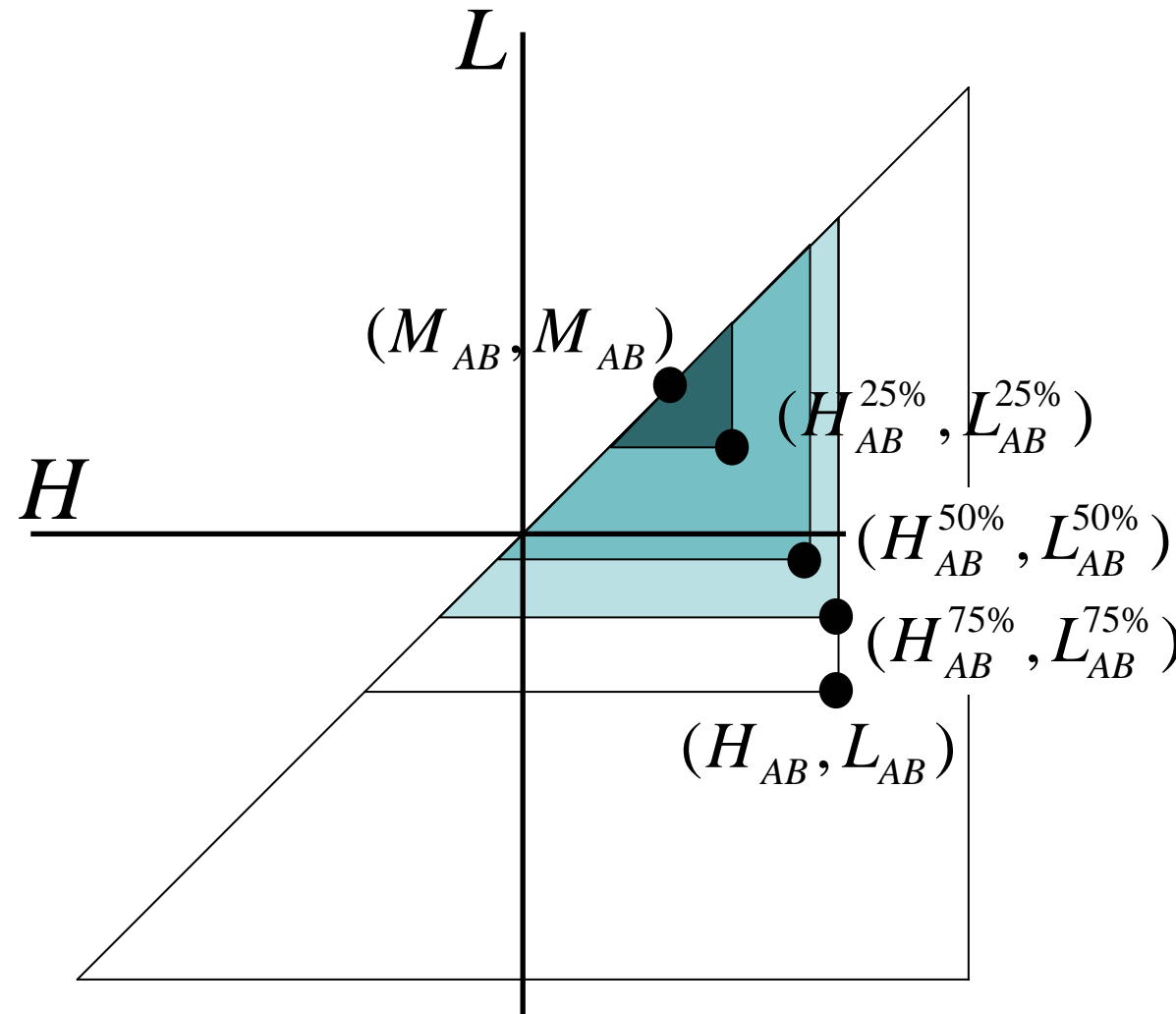
$$\lim_{x \rightarrow 100\%} H_{AB}^x \uparrow H_{AB}$$

x-Percentage Interval



- The 25% interval is $[0.1, 0.1]$
- The 50% interval is $[-0.1, 0.3]$
- The 75% interval is $[-0.4, 0.6]$
- The 100% interval is $[-0.6, 0.6]$

Authorization Indexes



L_{AB} and H_{AB}

M_{AB}

$L_{AB}^{25\%}$ and $H_{AB}^{25\%}$

$L_{AB}^{50\%}$ and $H_{AB}^{50\%}$

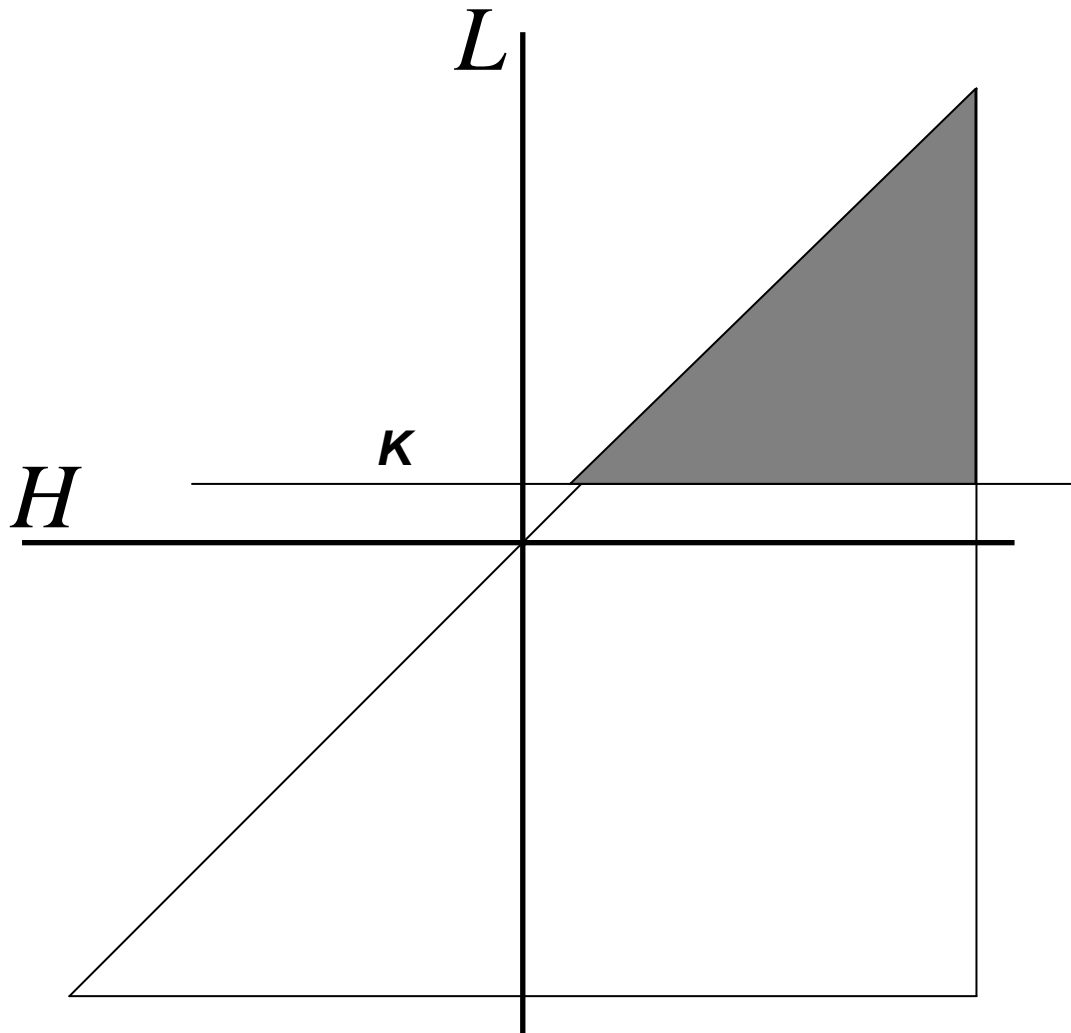
$L_{AB}^{75\%}$ and $H_{AB}^{75\%}$

Authorization Policies Principles

- Worst path. Grant If $L_{AB} \geq K$
- Best path. Grant if $H_{AB} \geq K$
- Mean index. Grant if $K_1 \leq M_{AB} \leq K_2$

$$L_{AB} + H_{AB} \geq 2K$$

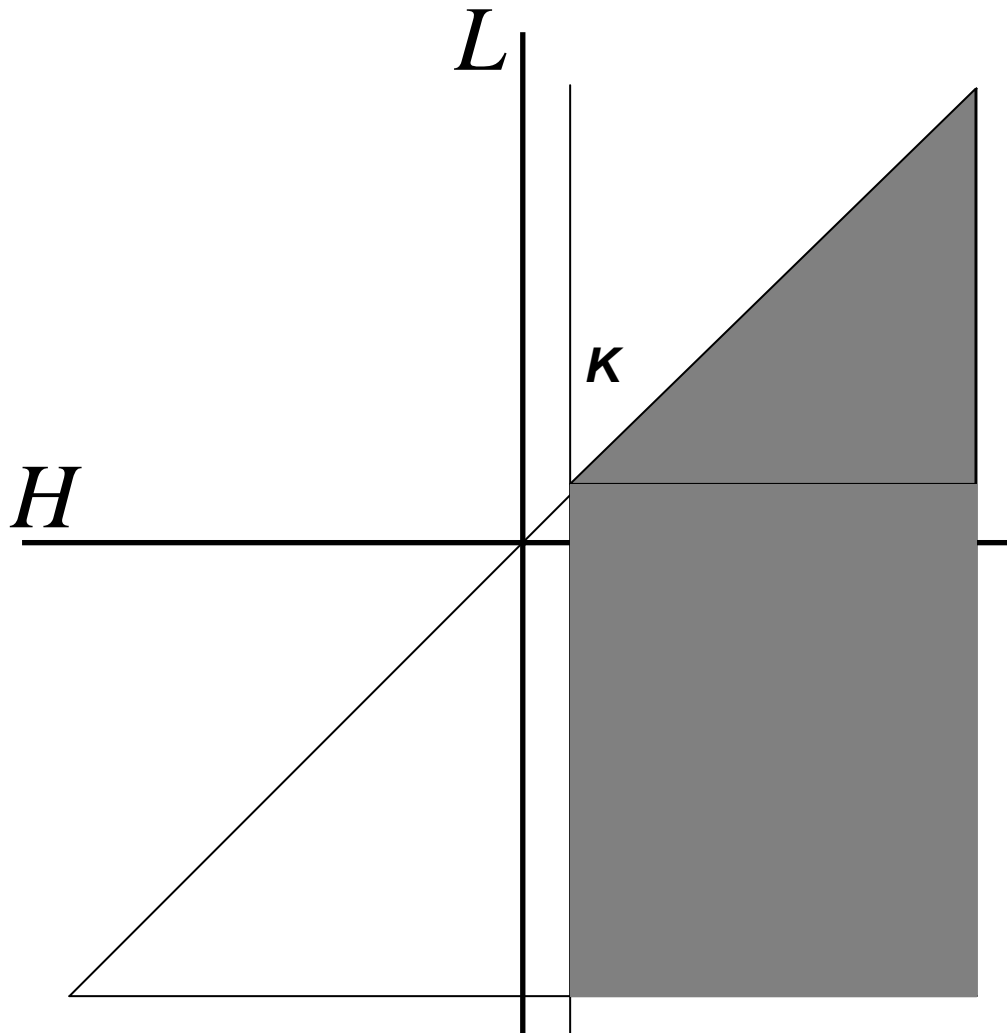
Authorization Policies



$$L_{AB} \geq K$$



Authorization Policies

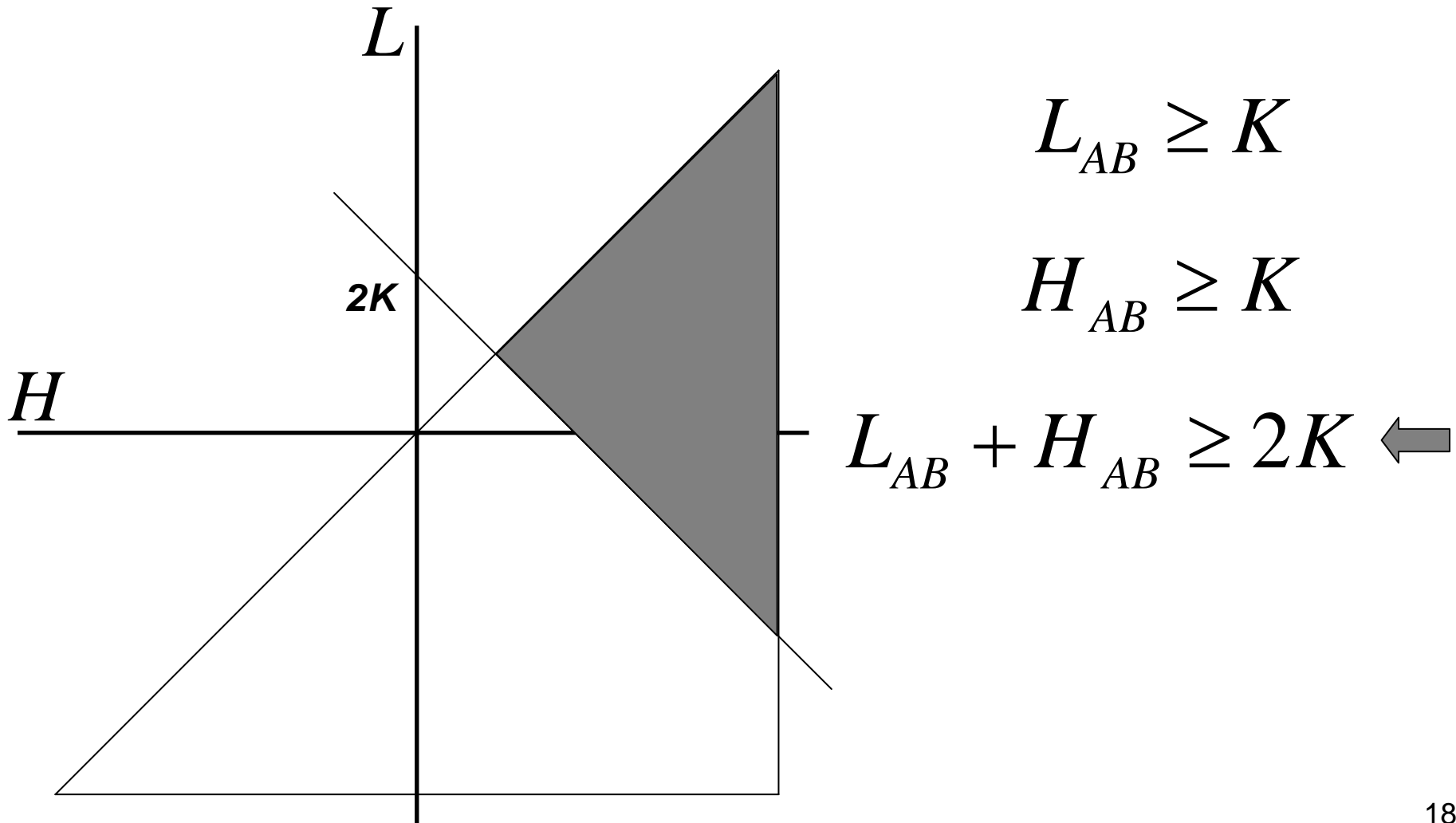


$$L_{AB} \geq K$$

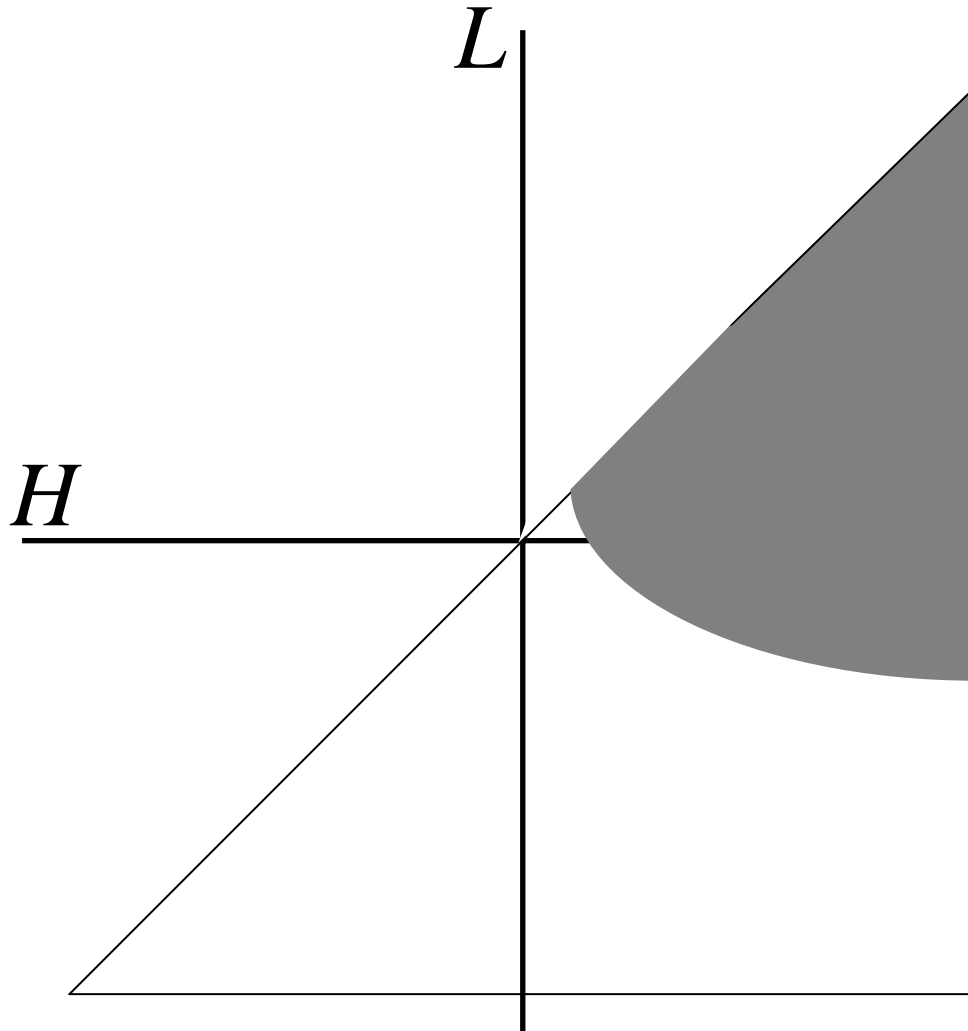
$$H_{AB} \geq K$$



Authorization Policies



Authorization Policies



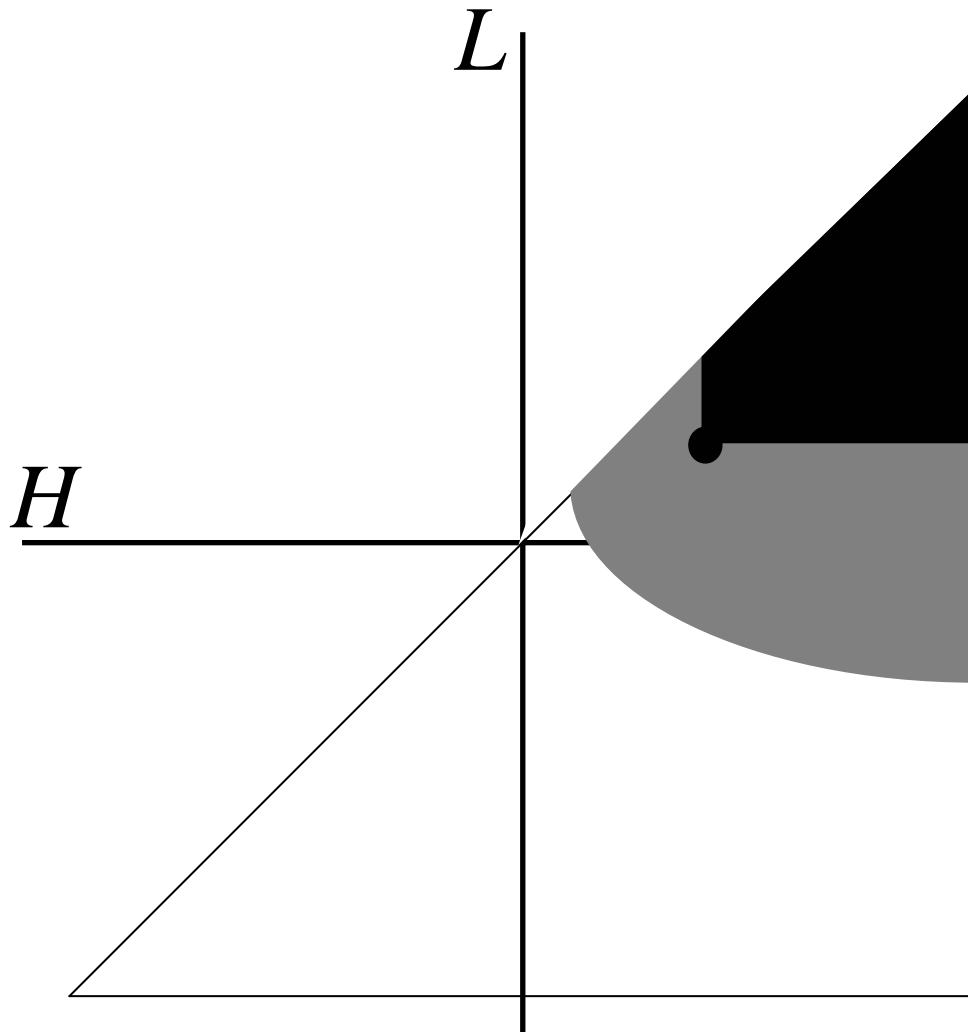
$$L_{AB} \geq K$$

$$H_{AB} \geq K$$

$$L_{AB} + H_{AB} \geq 2K$$

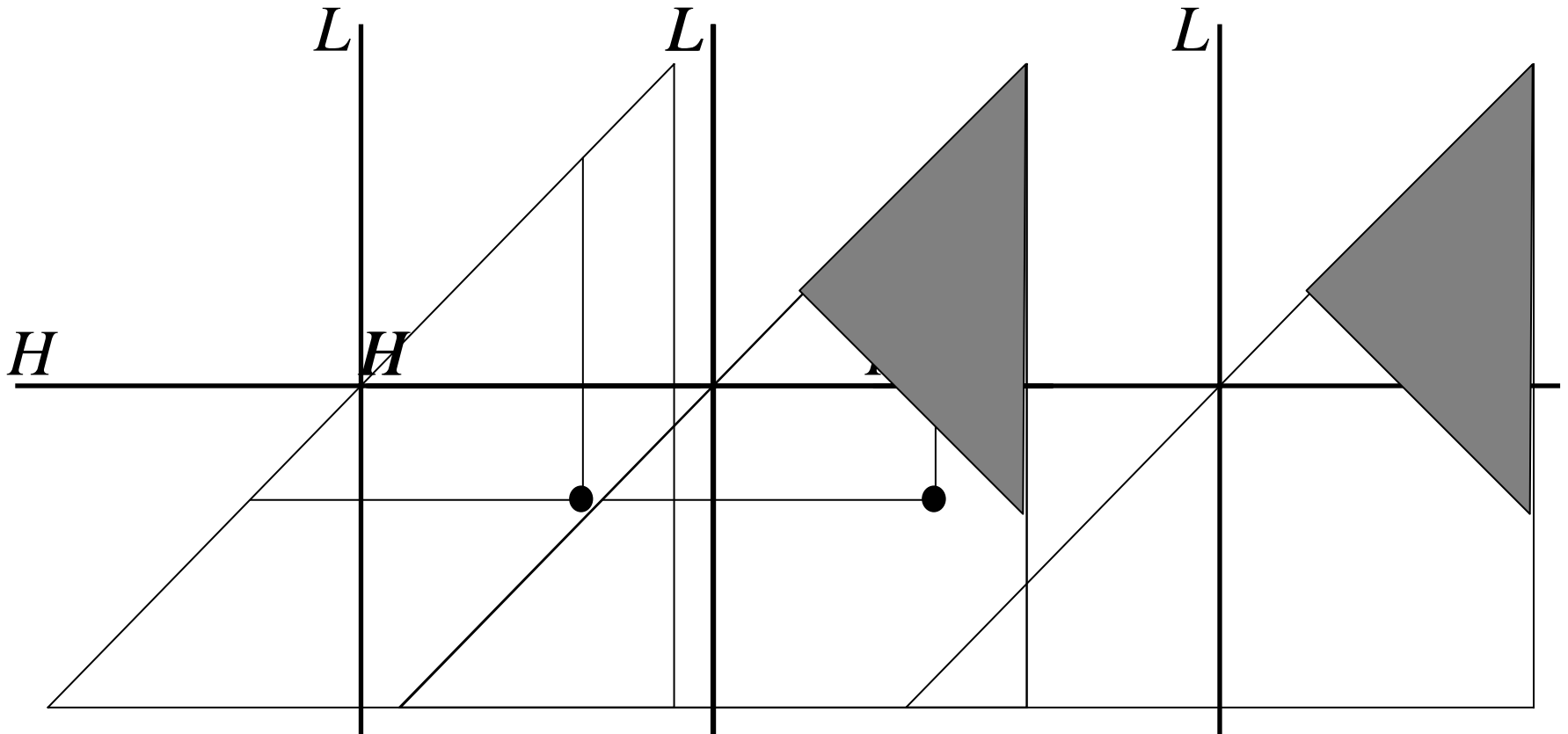
General Set ←

Authorization Set



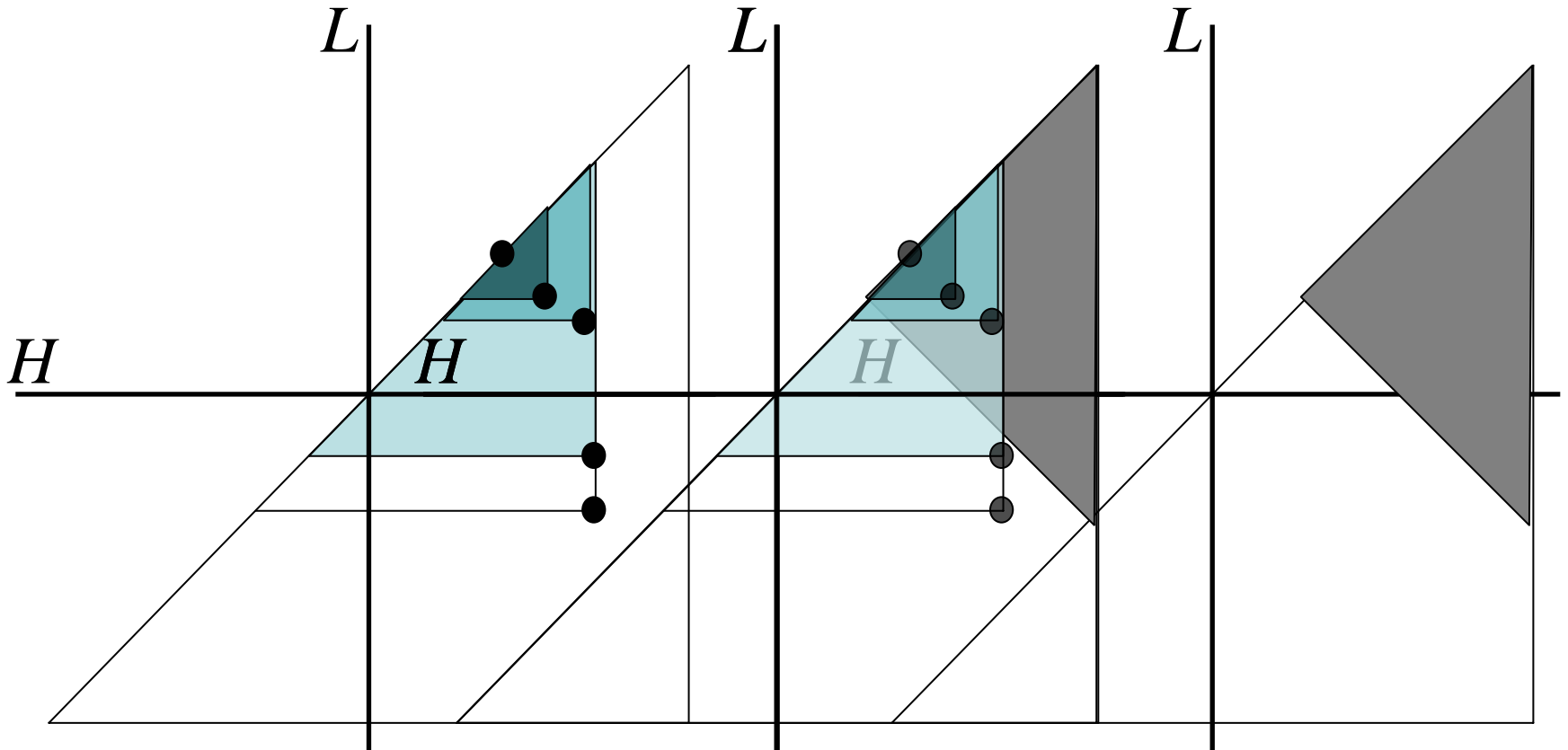
- Included in the triangle $(1,1), (1,-1), (-1,-1)$
- if (h,l) in S , then (h',l') in S for $h' \geq h$ and $l' \geq l$

Authorization Policies



Authorization Denied because $(H_{AB}, L_{AB}) \notin P$

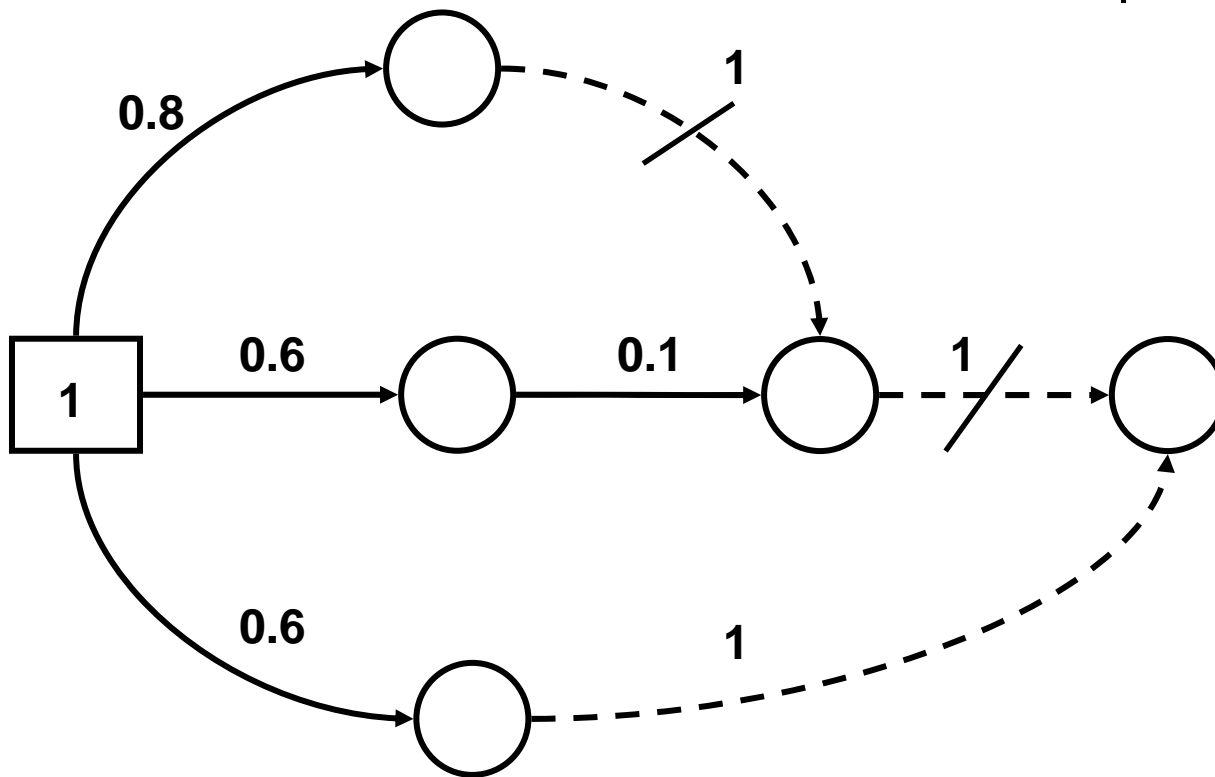
Authorization Policies



Authorization Granted at 50 % because $(H_{AB}^{50\%}, L_{AB}^{50\%}) \in P$

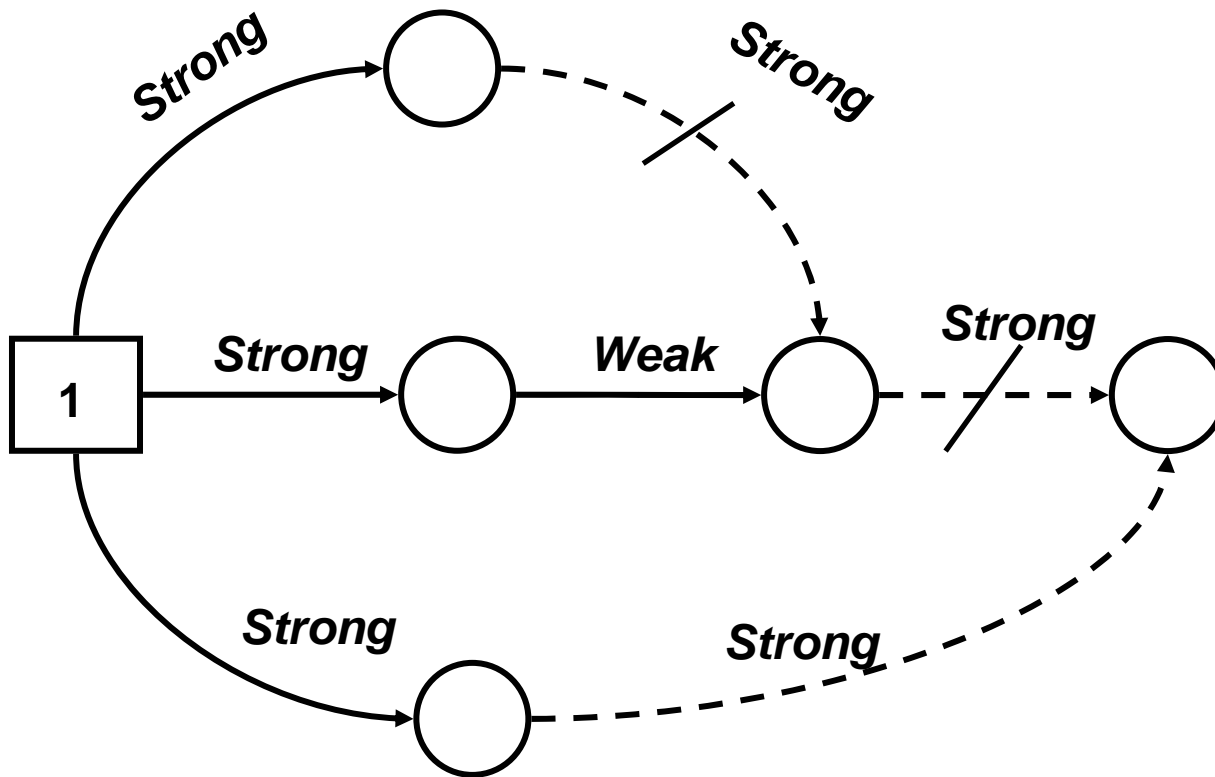
Security Level Policy

$$|m| > 0.5$$



Security Level Policy

$|m| > \text{Strong}$



Strong = 1
Weak = 0.5

